

**First Year B.Sc (MRT) Degree Examinations - July 2015**

**Mathematics**

**Time: 3 Hours**

**Total Marks: 100**

- Answer all Questions.
- Draw Diagrams wherever necessary.

**Essay**

**(2x20=40)**

1. a) Differentiate  $\sqrt{3x+2} + 1/\sqrt{2x^2+4}$   
 b) If  $x^y = e^{(x-y)}$  Show that  $dy/dx = \log x / (1 + \log x)^2$ .  
 c) Integrate  $1/(\sqrt{81+64x^2})$   
 d) Integrate  $(e^x (x+1))/(x+2)^2$
2. a) Find correlation coefficient  

X:	1	3	5	6	8	10	12
Y:	2	6	8	10	14	16	19

  
 b) Write properties of normal distribution  
 c) For a binomial distribution mean= 12, variance=4, Find  $P(X=2)$

**Short notes:**

**(8x5=40)**

3. Show that the matrix  $A = \begin{bmatrix} 3 & 1 & 0 \\ 1 & 2 & -1 \\ 4 & -3 & 1 \end{bmatrix}$  is non singular.
4. Show that  $\cos 2\theta = (1 - \tan^2 \theta) / (1 + \tan^2 \theta)$ .
5. If  $y = 3e^{2x} + 2e^{3x}$ , Show that  $d^2y/dx^2 - 5 dy/dx + 6y = 0$ .
6. Integrate  $4x / ((x-2)(x-1))$
7. Find the angle between two lines AB and AC where  $A=(1,4,3)$ ,  $B=(2,3,2)$ ,  $C=(5,2,6)$  in a cartesian plain.
8. Derive the Euler formula  $e^{ix} = \cos x + i \sin x$
9. Show that  $\sin A + \sin (120+A) + \sin(240+A) = 0$
10. From an urn containing 5 white and 7 black balls, 2 balls were selected randomly. What is the probability that both are (1) same colour (2) different colour.

**Answer briefly:**

**(10x2=20)**

11. Write a general form of fourier series.
12. When a matrix is said to be symmetric.
13. Define non –singularity of a matrix.
14. When did a set of vector are said to be linearly independent.
15. Sum of 1<sup>st</sup> 3 terms of an AP is 30 and the difference between 3<sup>rd</sup> and 1<sup>st</sup> term is 12. Find the terms.
16. Find  $\sin (22 \frac{1}{2}^\circ)$
17. Find  $\lim ((2+n)(3+n^2)/((n^2+1)(2n+1))$  as n tends to infinity.
18. Write down Simpson's 1/3<sup>rd</sup> rule for numerical integration.
19. Find a.b , where  $a=i+2j-3k$ ,  $b=2i-4j+6k$ .
20. Give an example of 1<sup>st</sup> order differential equations.

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